## FALL 24 - CALCULUS 3 - EXAM 4A - Solutions

No references. True or false...polar coordinates are  $(r, \theta)$ , cartesian coordinates are (x, y, z), cylindrical coordinates are  $(r, \theta, z)$  and spherical coordinates are  $(\rho, \theta, \phi)$ . Assume all integrals exist.

F 1) 
$$\frac{\partial(r,\theta)}{\partial(x,y)} = r$$

F 2) 
$$\frac{\partial(r, \theta, z)}{\partial(x, y, z)} = r$$

T 3) 
$$\frac{\partial(x, y, z)}{\partial(\rho, \theta, \phi)} = \rho^2 \sin \phi$$

F 4) 
$$\frac{\partial(x, y, z)}{\partial(r, \theta, z)} = r$$

T 5) There are six different ways to write the same triple integral

$$\mathsf{F} \mathbf{6} \int_{a}^{b} \int_{c}^{d} f(x, y) dx dy = \int_{a}^{b} \int_{c}^{d} f(x, y) dy dx$$
$$\mathsf{T} \mathbf{7} \int_{y} \int_{x} f(x, y) dx dy = \int_{\theta} \int_{r} f(x(r, \theta), y(r, \theta) r dr d\theta$$

F 8) In polar coordinates  $x = r \cos \phi$ 

F 9) In spherical coordinaters  $z = \rho \cos \theta$ 

F 10) 
$$\rho = r$$

- T 11) The equation of a cylinder in cylindrical coordinates could be r = a, some constant
- F 12) The equation of a sphere in spherical coordinates could be r = a, some constant
- F 13) The centroid and the center of gravity never coincide if density is not constant
- F 14) The centroid of a figure depends on its density
- F 15) The center of mass of a three dimensional body always lies on its axes of symmetry

F 16) The centroid and center of mass are the same thing

T 17)  $M_{xy}$  is the moment of the mass of an object relative to the xy plane

F 18)  $M_{yz}$  is the moment of inertia of a mass about the yz plane

T 19) Differential moment of inertia of a differential mass dm about the z-axis is  $dI = (x^2 + y^2)dm$ 

T 20) A rectangle has a higher moment of inertia around its shorter side than its longer side

T 21) Jacobians are local area or volume magnification factors for double or triple integrals

F 22) The equation of a paraboloid in cartesian coordinates could be  $x^2 + y^2 = z^2$ 

T 23)  $\iiint f(x, y, z) | dx dy dz \ge \iiint f(x, y, z) dx dy dz$ 

T 24) Coordinate transformations must be bijective mappings

T 25) The polar moment of inertia  $I_0$  of a figure in the xy plane is the sum  $I_x + I_y$