

①

10/3

Derivative of e^x and e^{kx} , k constant

$$\frac{d}{dx}(e^x) = \underline{e^x}$$

$$\frac{d}{dx}(e^{kx}) = \underline{e^{kx}} \cdot k = ke^{kx}$$

Ex: $F = Pe^{rt}$

$$\begin{aligned} \frac{dF}{dt} &= ? = P \cdot r e^{rt} = (rP)e^{rt} \\ &= r(Pe^{rt}) \end{aligned}$$

$$\frac{dF}{dt} = rF$$

$$a^x = \left[\underset{\substack{\uparrow \\ a}}{e^{\ln a}} \right]^x = e^{x \ln a}$$

$$\frac{d(a^x)}{dx} = (\ln a) e^{x \ln a} = (\ln a) a^x$$

(2)

$$\textcircled{*} \frac{d}{dx} (e^{g(x)}) = \underline{e^{g(x)}} \cdot g'(x)$$

$$\text{Ex: } \frac{d}{dx} (e^{x^3+2x^2-5x}) = (e^{x^3+2x^2-5x}) (3x^2+4x-5)$$

$$\text{Ex: } f(x) = x^5 \cdot e^{2x} = x^5 (e^{2x})' + (x^5)' \cdot e^{2x}$$

Product Rule

$$= x^5 \cdot 2e^{2x} + 5x^4 \cdot e^{2x}$$

$$= \underline{x^4 e^{2x} [2x+5]}$$

$$\text{Ex: } f(x) = \frac{e^{5x}}{3x-1} \quad \text{Want } f'(x) = ?$$

$$f'(x) = \frac{(3x-1)(5e^{5x}) - (3)e^{5x}}{(3x-1)^2}$$

3

For U^{239}

Start w/
100g.

$$A(t) = 100e^{-0.362t}$$

(i) Find $A'(t)$

(ii) Find $A'(3)$

$$\begin{aligned} \text{(i) } A'(t) &= (100)(-0.362)e^{-0.362t} \\ &= -36.2e^{-0.362t} \quad (\text{g/yr}) \end{aligned}$$

$$\text{(ii) } A'(3) = -12.2 \text{ g/yr}$$

p.258

#7

$$f(t) = 100^t \quad f'(t) = \ln(100) \cdot 100^t$$

#12

$$\begin{aligned} y &= 1.2e^{5x} \quad y'(x) = (1.2)(5e^{5x}) \\ &= 6e^{5x} \end{aligned}$$

④

#31 $f(z) = (2z + e^{-z^2})^2$

$$f'(z) = 2(2z + e^{-z^2}) \cdot (2z + e^{-z^2})'$$

↑ harder

$$= 2(2z + e^{-z^2}) \cdot [2 + e^{-z^2} \cdot (-2z)]$$

#42 $f(x) = e^{\left(\frac{x^2}{x^3+2}\right)}$

$$f'(x) = e^{\left(\frac{x^2}{x^3+2}\right)} \cdot \left[\frac{x^2}{x^3+2}\right]'$$

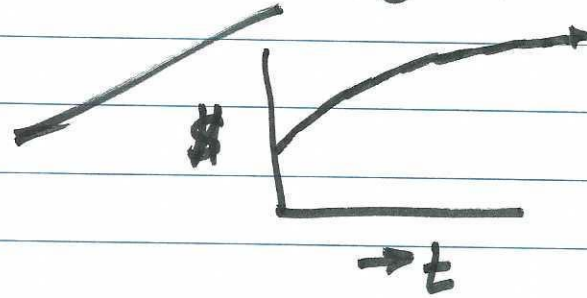
$$= e^{\left(\frac{x^2}{x^3+2}\right)} \cdot \left[\frac{(x^3+2)(2x) - (x^2)(3x^2)}{(x^3+2)^2}\right]$$

(5)

#52 $S(t) = 100 - 90e^{-0.3t}$ $27e^{-0.9}$

(a) $S'(t) = 27e^{-0.3t}$

(b) $S'(5) = 27e^{-1.5}$



(c) Rate of sales increase declines

#56 $A(t) = 10t^2 2^{-t}$ # people aware of product after t months

%

(a) after 2 months:

$$A'(2): A'(t) = 10 \left[t^2 (\ln 2 \cdot 2^{-t}) + (2t \cdot 2^{-t}) \right]$$
$$= 10 \cdot 2^{-t} (t^2 \ln 2 + 2t)$$
$$= 10 \cdot \frac{1}{4} (4 \cdot 0.693 + 4)$$
$$= \frac{5}{2} (6.28) \sim > 0$$

$$A'(4) < 0$$

⑥

$$1) \frac{d}{dx} (\ln x) = \frac{1}{x}$$

$$2) \frac{d}{dx} (\log_a x) = \frac{1}{\ln a \cdot x}$$

$$3) \frac{d}{dx} (\ln g(x)) = \frac{g'(x)}{g(x)} \leftarrow \text{"relative change"}$$

$$4) \frac{d}{dx} (\log_a g(x)) = \frac{g'(x)}{g(x)} \cdot \frac{1}{\ln a}$$

Ex: $f(x) = 3x (\ln x^2) = (3x)(2 \ln x) =$

$$f'(x) = 6 \left[x \cdot \frac{1}{x} + (1)(\ln x) \right] \quad \underline{6x \ln x}$$

$$= 6 [1 + \ln x]$$

7

$$f(t) = 30,781 - 24,277 \log(0.46t + 1)$$

Find $f(8)$; $f'(8)$

$$\begin{aligned} f(8) &= 30,781 - 24,277 \log(8 \cdot 0.46 + 1) \\ &= 14,509 \end{aligned}$$

$$f'(t) = \frac{(-24,277) \cdot (0.46)}{(0.46t + 1)(\ln 10)} = -2$$

$$f'(8) = -103\%$$

$f(0) - f(8)$ is 8 yr depreciation

$f'(8)$ is annual rate of loss @ $t=8$